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OPTIMIZATION METHODS FOR ENGINEERS

N.V.S. Raju

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Dedicated to

My Wife

MRS PRASANNA LAKSHMI

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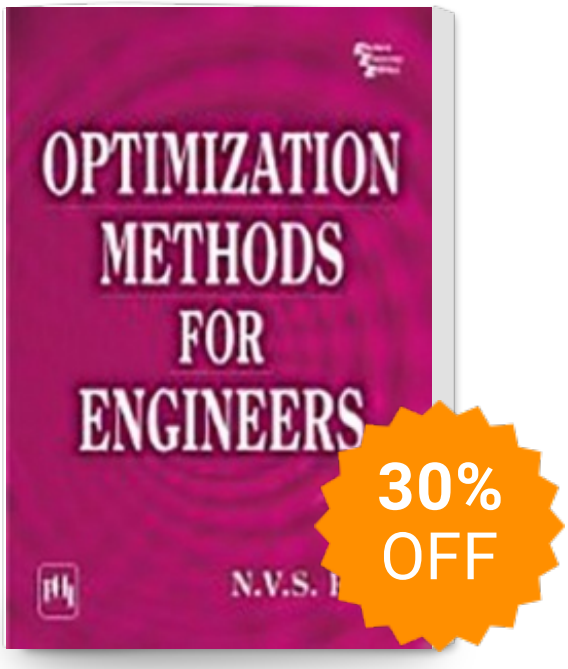

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